FDMM: A Formalism for Describing ADOxx Meta Models and Models

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Abstract: In the paper at hand we present the FDMM formalism that can be used to describe the core constituents of

the ADOxx meta modeling approach as it is provided for the Open Models Initiative (OMI). The formalism is based on a first-order logic setting. Thereby formal descriptions of the implementation of modeling languages based on ADOxx can be realized in an intuitive and mathematically exact format. To illustrate the use of the formalism it is applied to a modeling language and its instances from the area of risk management that has been previously implemented in ADOxx. It is then analysed how the concepts of the FDMM formalism compare to the ADOxx meta modeling concepts as well as other meta modeling approaches from the area of

domain-specific modeling.

1 INTRODUCTION

Conceptual models are today used in many areas of enterprise information systems (Kaschek, 2008; Karagiannis et al., 2008a; Wand and Weber, 2002). Examples range from fields such as strategic management, business process and workflow management to enterprise architecture and software engineering. For these purposes a large variety of modeling languages have been developed and successfully applied in academia and industry (Borgida et al., 2009). When it comes to the sharing of such modeling languages and their corresponding models - as it has been recently promoted by the Open Models Intiative (Koch et al., 2006; Karagiannis et al., 2008b) - the exact description of a modeling language and the models is one of the most important tasks. These descriptions not only reflect the design choices made during the implementation of the language. They also permit to compare and learn from different implementations of a modeling language and support the interpretation of the models (Hinkelmann et al., 2010).

In order to describe the building blocks of modeling languages it can be reverted to several types of *meta modeling* approaches (Kern et al., 2011). These approaches provide the constructs necessary for describing the abstract and concrete syntax of a modeling language (Harel and Rumpe, 2004; Karagiannis and Kuehn, 2002). In this way they also define constraints and correctness criteria for creating

valid models based on the definition of a modeling language. In the context of the Open Models Initiative, several projects¹ have reverted to the freely available and industry proven ADOxx² meta modeling approach. At its core, the ADOxx approach allows to specify the syntax of a modeling language together with its graphical representation. From these specifications, visual model editors are then created automatically (Kuehn, 2010).

For the description of ADOxx based modeling languages, it has so far either been reverted to natural language descriptions, e.g. (Bork and Sinz, 2010; Fill et al., 2007), concrete implementations in the form of source code, e.g. (Schwab et al., 2010; Nemetz, 2006) or visual representations, e.g. (Hofer, 2011; Braun and Winter, 2005). A formal description of the ADOxx meta modeling approach is so far not available. This is however necessary to analyze and evaluate how the syntax of a certain modeling language has been realized, compare ADOxx meta models and models to other meta modeling approaches such as GME, Ecore or ARIS cf. (Kern et al., 2011), derive suggestions for its enhancement and finally describe semantics for its further processing (Demirkan et al., 2008; Harel and Rumpe, 2004).

Therefore we propose the FDMM³ formalism that

¹See http://www.openmodels.at/web/omi/omp

²ADOxx is a registered trademark of BOC AG.

³The acronym FDMM stems from: A <u>F</u>ormalism for <u>D</u>escribing ADOxx <u>M</u>eta Models and <u>M</u>odels

is capable of describing the core constitutents of the ADOxx approach. FDMM aims to provide an easy to use formalism that does not require specialized mathematical knowledge and that is capable of expressing the implementation of ADOxx meta models and models. The paper is structured as follows: In section 2 we will briefly discuss the foundations of modeling languages, meta models and models, the characteristics of the ADOxx approach and describe a running example for a modeling language from the area of enterprise information systems. Section 3 will describe the formalism including the necessary constraints and correctness criteria. In section 4 the formalism will be applied to the sample modeling language. The result of this application is then discussed in section 5. Work related to the approach will be part of section 6. The paper is concluded by an outlook on the future work in section 7.

2 FOUNDATIONS

In this section we will briefly define the terms *modeling language*, *meta model* and *model* and describe the main characteristics of the ADOxx meta modeling approach. Finally, we will present a running example by using a modeling language from the area of risk management.

2.1 Modeling Language, Meta Model and Model

According to a framework proposed by (Karagiannis and Kuehn, 2002), a modeling language is composed of a syntax, semantics and notation. The syntax specifies the elements and attributes of the language and the semantics assigns meaning to these constructs. In contrast to other frameworks, the notation is treated separately and is used to specify the visual representation of the language. The syntax further consists of an abstract syntax, which is represented by the meta model, and the concrete syntax, which is represented by a model (Harel and Rumpe, 2000; Harel and Rumpe, 2004; Sprinkle et al., 2010). The meta model can itself be described by a modeling language, i.e. the meta modeling language. Accordingly, the abstract syntax of the meta modeling language is represented by a meta meta model and the concrete syntax is represented by a meta model (Kern et al., 2011).

An example for these relationships is shown in figure 1: in the meta meta model the two entities *element* and *attribute* are defined. Additionally, a relation between the two entities is shown. On the meta model level the E_1 entity is defined as an element and the A_1

and A_2 entities as attributes that can be related to E_1 . Finally, on the model level the entities ε_1 and ε_2 are defined as E_1 elements, the α_1 and α_2 entities as A_1 attributes and the β_1 and β_2 entities as A_2 attributes. The meta meta model thus defines which entities are provided for the specification of the abstract syntax of a modeling language in the form of a meta model. If the specification of the meta meta model is generic enough it can be used to specify a multitude of different modeling languages. A typical use case is then to automatically create model editors based on the static meta meta model specification and the dynamically adaptable meta model specifications.

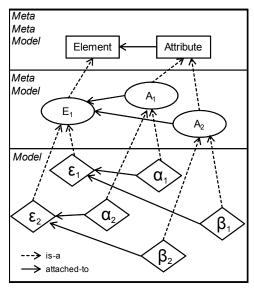


Figure 1: Example for a Meta Model, a Meta Model and a Model

In addition to association mechanisms for defining linkages between entities, meta meta models typically also provide inheritance and containment mechanisms (Sprinkle et al., 2010). By inheritance mechanisms, generalization and specialization relationships between entities of a meta model can be expressed to provide means for effecting polymorphic behaviors at model execution or interpretation time. This is required in particular for the design of algorithms that shall work on multiple, similar modeling languages without the need of particular adaptations: by defining an algorithm on a set of general entities that are shared by different meta models, the algorithm can be later bound automatically to entities that are inherited from these general entities. Containment mechanisms refer to the inclusion of a set of entities into another entity on the model level. This is typically used to specify model/diagram types or aggregations/nestings that group sets of entities.

2.2 The ADOxx Meta Modeling Approach

The ADOxx meta modeling approach has originally been conceived in the course of the development of the ADONIS business process management toolkit in 1995. Since then it has been successfully used in a large number of academic and commercial projects by more than 1000 customers worldwide (Harmon, 2010; Junginger et al., 2000). The basic building blocks of its meta meta model are classes and relationclasses that are complemented with attributes (Junginger et al., 2000). Classes are organized in the form of an inheritance hierarchy so that the attributes of a super-class are inherited by its subclasses in the sense of standard object orientation principles. Relationclasses are defined by their fromclass and to-class attributes to specify valid instances of source and target classes. These relations can be complemented with cardinality constraints to limit the number of participating instances.

For collections of classes and relationclasses a containment mechanism in the form of *model types* is available. Model types define the context for the instantiation of classes and relationclasses in the form of *models*. Therefore, when creating a model, at first a model type has to be selected to specify which classes and relationclasses are valid in a model. Subsequently, these classes and relationclasses are instantiated as part of the model.

Besides the standard data types such as integer, string, and double, enumeration attributes are available in ADOxx that contain pre-defined values that can only be selected but not modified by a user during modeling. Furthermore, attributes can also be of two special types: attributes of the type expression contain strings in a proprietary expression grammar for automatically calculating the value of an attribute. Attributes of the type interref allow linking the instance of a class to another class instance of the same or of a different model instance or linking it to the same or a different model instance itself. The graphical representation of the instances of classes and relationclasses is specified via the particular string attribute named GRAPHREP. This attribute permits to specify context-dependent graphical representations for the classes and relationclasses, again based on a proprietary grammar - cf. (Fill, 2009). Although an inherent part of the ADOxx approach, the graphical representation can thus be modified independently from the other entities.

With these characteristics, the following requirements were defined for a formalism that can describe the concepts of the ADOxx meta modeling approach:

It should permit a formal description of the approach that is easy to handle and thus suitable for a wide range of users. Therefore, the formalism should focus on the core constituents to enable the description of arbitrary modeling languages that have been implemented using the ADOxx approach. It should however be extensible to allow its further development and future refinement.

2.3 Running Example: The 4R Modeling Language

As a running example we will revert to an existing modeling language in enterprise information systems from the area of governance, risk, and compliance (GRC). This example will first illustrate how meta models and models are typically used in information systems to create domain conceptualizations. In section 4 we will revert to it again for showing the application of the FDMM formalism.

In the last years particular consideration has been given to the management of risks and regulatory compliance together with their effects on returns and corresponding reporting requirements of enterprises. In line with these developments, the framework for integrated enterprise balancing has been derived (Faisst and Buhl, 2005; Fill et al., 2007; Gericke et al., 2009). The goal of this framework is to govern business activities with organization-wide consistent return and risk indicators. As a foundation, it is necessary to provide a common data basis that represents information from the areas of risk, return, regulation, and reporting - the so-called 4R information architecture. For acquiring this information, the 4R modeling language (Fill et al., 2007) and the 4R situational method for implementing such solutions in an organization were developed (Gericke et al., 2009). In its original form, the central parts of the 4R modeling language were illustrated by an extension of a graph based formalism. The corresponding realization using the ADOxx meta modeling approach was however described in natural language.

The meta model of the 4R modeling language, as it was specified in ADOxx, contains the following model types (Fill et al., 2007): the 4R portfolio model, the 4R business process model, and the 4R organizational model. Briefly summarized, the portfolio model type is used to describe multi-dimensional aggregations of the risks, returns and correlations of business transactions in regard to their relations to products and customers (Faisst and Buhl, 2005). The single business transactions in this model can be linked to instances of the 4R business process model type. This second model type extends the process

modeling language of business graphs (Karagiannis et al., 1996) with elements, relations, and attributes for representing events, aggregations of events and their influence on the properties of process activities. The meta model is complemented with a 4R organizational model for representing actors, organizational units, resources, and roles that fulfill tasks in a business process.

For the implementation of the 4R model types on ADOxx the following classes and relationclasses together with several attributes were specified to represent the risk and return figures of business transactions and the underlying risk-affected business processes:

- for the portfolio model type the class *business transaction* and the relationclass *relates business transaction*,
- for the 4R business process model the super class FlowObject and as sub classes of this class: Start, Decision, SubProcess, Activity, Parallelity, Join, and End. Additionally the classes: 4R risk aggregation, and 4R event; the relationclasses: subsequent, 4R aggregation relation, and 4R influences relation
- for the 4R organizational model the classes: *actor*, *organizational unit*, *resource*, and *role*; and the relationclasses: *uses resouce*, *belongs to unit*, *has role*, and *has resource*

To apply the FDMM formalism we will later regard the 4R portfolio model and the 4R business process model type in more detail. The classes and relation classes of these model types are represented by the sets of symbols as shown in figure 2.

3 THE FDMM FORMALISM

As stated in the introduction, the goal of this paper is to develop a formalism that is capable of describing the core constituents of ADOxx meta models and models as well as the criteria for valid models based on the meta model definitions. FDMM is therefore not a formalization of all aspects of the ADOxx approach, but a formalism that aims to support users of ADOxx to describe their meta models and models in a formal way. For the development of the formalism we reverted both to literature sources on the ADOxx meta modeling approach as well as existing implementations (Karagiannis et al., 2008a; Fill, 2009; Kuehn, 2010). During the development we aimed for keeping the formalism as simple as possible while not sacrificing any of the core concepts of the approach.

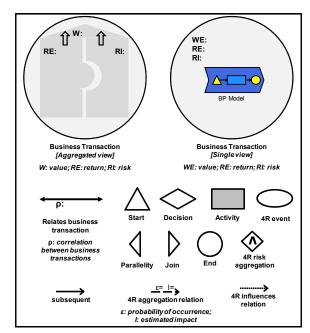


Figure 2: Symbols of the 4R Portfolio Model Type and the 4R Business Process Model Type

3.1 Definition of Meta Models

At first we define the basic constituents of meta models **MM** which can then be used to derive model instances **mt**. We define a meta-model to be a tuple of the form

$$\mathbf{MM} = \langle \mathbf{MT}, \preceq, \mathbf{domain}, \mathbf{range}, \mathbf{card} \rangle \tag{1}$$

where

• MT is the set of model types. We have

$$\mathbf{MT} = \{\mathbf{MT}_1, \mathbf{MT}_2, \dots, \mathbf{MT}_m\}$$
 (2)

where \mathbf{MT}_i in turn is a tuple,

$$\mathbf{MT}_i = \langle \mathbf{O}_i^T, \mathbf{D}_i^T, \mathbf{A}_i \rangle \tag{3}$$

consisting of the set of object types \mathbf{O}_i^T , a set of data types \mathbf{D}_i^T , and a set of attributes \mathbf{A}_i . In this way ADOxx classes and relationclasses are uniformly represented as object types. As will be described below we will use the attributes \mathbf{A}_i also for expressing associations between object types. When we describe the instantiation of the meta model in section 3.2 in model instances, the attributes will map the instantiation of object types to the instantiation of either object types or data types. This permits us to represent the ADOxx concepts of relationclasses and interref relations in the same way. However, this also means that, if for example directed relations are required, the notions of source and target object types have

to be added when specifying a particular meta model. The object types, data types, and attributes are part of their respective total sets:

$$\mathbf{O}^{T} = \bigcup_{j} \mathbf{O}_{j}^{T}, \mathbf{D}^{T} = \bigcup \mathbf{D}_{i}^{T}, \mathbf{A} = \bigcup \mathbf{A}_{i}$$
 (4)

- \leq is an ordering on the set of object types, \mathbf{O}^T . If $o_1^t \leq o_2^t$ we say that the object type o_1^t is a subtype of the object type o_2^t . Thereby the inheritance hierarchy of ADOxx classes can be expressed. Due to the generic definition, this ordering can also be used for relationclasses: as ADOxx requires a from-class and a to-class attribute for relation-classes, a generic object type with these attributes can be defined and used for the definition of subtypes that inherit these attributes.
- the domain function maps attributes to the power set of all object types, i.e.

domain:
$$\mathbf{A} \to \mathcal{P}(\bigcup_{j} \mathbf{O}_{j}^{T})$$
 (5)

The domain function will constrain what objects an attribute can map in the model instances. It is therefore used to attach attributes to a particular set of object types. In regard to ADOxx this corresponds to the assignment of ADOxx attributes to classes and relationclasses and the definition of an endpoint of an ADOxx relationclass.

 The range function maps an attribute to the power set of all pairs of object types and model types, all data types, and all model types

range:
$$\mathbf{A} \to$$
 (6)
$$\mathcal{P}\left(\bigcup_{j} (\mathbf{O}_{j}^{T} \times \{\mathbf{MT}_{j}\}) \cup \mathbf{D}^{T} \cup \mathbf{MT}\right)$$

In the model instances, the range function will constrain what values an attribute can take. For the definition of a meta model it is thus used to specify the type of an attribute. I.e. whether the attribute has the function of specifying the relation of an instance of an object type in a model instance to either: a. the instances of object types in a particular model type, b. instances of data types or c. instances of model types. Case a. thus corresponds to both the relationclass and interref concepts in ADOxx that have an instance of a class as a target, case b. to the ADOxx attribute concepts except interref attributes, and case c. to the ADOxx interref attribute concept that has an instance of a model type as a target.

 The card function maps pairs of object types and attributes to pairs of integers

card:
$$O^T \times A \to \mathcal{P}(\mathbb{N} \times (\mathbb{N} \cup \{\infty\}))$$
 (7

where $\mathbb N$ is the set of non-negative integers. In the model instances the card function will constrain how many attribute values a object can have. In regard to the different types of attributes this thus permits to specify how many instances of object types, of data types or of model types an attribute can contain. When comparing this to the ADOxx approach, the card function determines whether the value of an attribute corresponds to either: a. a target of a relationclass - that can only be one distinct class, b. the target of an interref attribute that can have multiple values or c. the instance of a datatype that can also have multiple values, which corresponds to the enumeration attribute type in ADOxx.

In addition we define the following correctness criteria for meta models: The sets of object types, data types, and attributes have to be pairwise disjoint

$$\mathbf{O}^T \cap \mathbf{D}^T = \emptyset, \ \mathbf{O}^T \cap \mathbf{A} = \emptyset, \ \mathbf{D}^T \cap \mathbf{A} = \emptyset$$
 (8)

This follows from the fact that in mathematical terms we have so far only been defining various sets that could overlap. In addition, for any attribute a that is part of the attribute set \mathbf{A}_i of the i-th model type - see equation 3, the domain function for that attribute must point to any of the object types in that model type

$$a \in \mathbf{A}_i \Rightarrow \operatorname{domain}(a) \subseteq \mathbf{O}_i^T$$
 (9)

That ensures that attributes that are related by the domain function to a certain object type are part of the same model type definition. This corresponds directly to the ADOxx approach in the way that all concepts that are relevant for the definition of models are grouped within the context of a model type.

3.2 Instantiation of Meta Models

We will now describe the instantiation of a meta model. The instantiation of a meta model essentially describes the mapping of the model types, object types, and data types to model instances, objects, and data values together with a set of triples. Thus, an instantiation of a metamodel **MM** will be a tuple

$$\langle \mu_{\mathbf{mt}}, \mu_{\mathbf{O}}, \mu_{\mathbf{D}}, \mathcal{T}, \beta \rangle$$
 (10)

where

• μ_{mt} is a one-to one mapping from model types to the power set of model instances:

$$\mu_{\mathbf{mt}}: \mathbf{MT} \to \mathcal{P}(\mathbf{mt})$$
 (11)

Thereby it is defined that a model instance must be of one specific model type and that there may be several instances of one model type. μ_O is a function taking the object types in a given model type to collections of objects:

$$\mu_{\mathbf{O}}: \bigcup_{j} \left(\mathbf{O}_{j}^{T} \times \{\mathbf{MT}_{j}\} \right) \to \mathcal{P}(\mathbf{O})$$
(12)

where

$$\mathbf{O} = \bigcup_{j} \mu_{\mathbf{O}}(\mathbf{O}_{j}^{T} \times \{\mathbf{MT}_{j}\})$$
 (13)

Thereby, the objects are defined as instances of an object type \mathbf{O}_{j}^{T} that is part of a particular model type \mathbf{MT}_{j} - see also equation 3. The addition of the model type is necessary as object types may be part of multiple model types and in the ADOxx approach objects can only occur within a model instance.

Sometimes it is convenient to create an object type which is meant to be subtyped but which is not meant to be directly instantiated. The purpose of such a type is to capture information that is common to all the subtypes. Such a type is called an *abstract type* and we can define what it means to be an abstract type based on the definitions above. An object type

$$o^t \in \mathbf{O}^T$$

is said to be abstract if for all model types \mathbf{MT}_i which contain the object type o^t ($o^t \in O_i^T$) we have

$$\mu_{\mathbf{O}}(o^t, \mathbf{MT}_i) = \bigcup_{o_1^t \neq o^t, o_1^t \leq o^t} \mu_{\mathbf{O}}(o_1^t, \mathbf{MT}_i).$$

That is to say that all the objects that instantiate o^t must instantiate o^t through one of its subtypes. In terms of ADOxx the notion of abstract types corresponds to super classes of which one or more of their sub classes are included in a model type but who cannot be instantiated themselves.

 \bullet $\mu_{\mathbf{D}}$ maps data types to a power set of data objects

$$\mu_{\mathbf{D}}: \mathbf{D}^T \to \mathcal{P}(\mathbf{D})$$
 (14)

The data types are not further constrained. It is thus left to the user of the formalism to ensure the correct content of a type, e.g. whether an 'integer' type contains only integer numbers. The formalism will only ensure that a data object is assigned a type that is valid in a particular context.

- $\mathcal{T} \subseteq \mathbf{O} \times \mathbf{A} \times (\mathbf{D} \cup \mathbf{O} \cup \mathbf{mt})$ is a set of triples. These triples will later be used to describe the contents of model instances.
- $\beta : \mathbf{mt} \to \mathcal{P}(\mathcal{T})$. This map describes how the triples are assigned to the model instances.

We will additionally define a collection of correctness constraints on the instantiation of the meta model. These constraints fall into two categories:

disjointness constraints that describe how a model instance is partitioned and domain/range/cardinality constraints that constrain how attributes can map objects to other objects and data values.

The following constraints define the disjointness and partitioning constraints that must be enforced for the various parts of the meta model instantiation:

 The instances of object types and the instances of datatypes must be disjoint, i.e. instances of object types and instances of datatypes cannot be the same.

$$\mu_{\mathbf{O}}(o^t, MT_i) \cap \mu_{\mathbf{D}}(d^t) = \emptyset$$
 (15)

 The instances of two object types are disjoint if either the object types are disjoint or if their model types to which they belong are disjoint, i.e. the formalism does not permit the instantiation from multiple object types nor a 'reuse' of objects of the same object type for different model instances:

$$i \neq j \lor o_1^t \neq o_2^t \Rightarrow$$

 $\mu_{\mathbf{O}}(o_1^t, \mathbf{MT}_i) \cap \mu_{\mathbf{O}}(o_2^t, \mathbf{MT}_j) = \emptyset$ (16)

• For two different model types \mathbf{MT}_i and \mathbf{MT}_j also the corresponding model instances must be disjoint, i.e. also for model instances no instantiations from multiple model types are allowed:

$$\mathbf{MT}_{i} \neq \mathbf{MT}_{j} \Rightarrow \mu_{\mathbf{mt}}(\mathbf{MT}_{i}) \cap \mu_{\mathbf{mt}}(\mathbf{MT}_{j}) = \emptyset$$
 (17)

 Every element of the set of model instances mt has to be derived from a model type, i.e. there cannot be model instances without a corresponding model type:

$$\mathbf{mt} = \bigcup \mu_{\mathbf{mt}}(\mathbf{MT}_j) \tag{18}$$

• For two different data types it must follow that also their instances are disjoint, i.e. also for data types it is not allowed that instances can be derived from multiple types:

$$d_1^t \neq d_2^t \Rightarrow \mu_{\mathbf{D}}(d_1^t) \cap \mu_{\mathbf{D}}(d_2^t) = \mathbf{0}$$
 (19)

T is the disjoint union of β(mt_i) where mt_i ∈ mt.
 More colloquially every triple is contained in exactly one model instance.

The following constraints define the inheritance, domain, range and cardinality constraints that the meta model instantiation must satisfy:

• if the object type $o_1^t \in \mathbf{O}_j^T$ is a subtype of the object type $o_2^t \in \mathbf{O}_j^T$ ($o_1^t \leq o_2^t$) then we have

$$\mu_{\mathbf{O}}(o_1^t, \mathbf{MT}_i) \subseteq \mu_{\mathbf{O}}(o_2^t, \mathbf{MT}_i).$$
 (20)

• Sibling object types are disjoint. More specifically if $o_1^t, o_2^t, o_3^t \in \mathbf{O}_i^T$ are object types such that

$$o_2^t \leq o_1^t, o_3^t \leq o_1^t,$$

 $o_2^t \not\leq o_3^t, o_3^t \not\leq o_2^t$

then

$$\mu_{\mathbf{O}}(o_2^t, \mathbf{MT}_i) \cap \mu_{\mathbf{O}}(o_3^t, \mathbf{MT}_i) = \emptyset.$$
 (21)

If the value y of a statement is an object, i.e. there is a mapping from an object type to an object for a concrete model type MT_j, then the pair of an object type and a model type have to be part of the range definition in the meta model:

$$(o^t, \mathbf{MT}_j) \in \operatorname{range}(a)$$
 (22)
 $(x \ a \ y) \in \mathcal{T} \land y \in \mathbf{O} \Rightarrow$

$$\exists o^t, MT_i, y \in \mu_{\mathbf{O}}(o^t, MT_i)$$
 (23)

The second equation further defines that if y points to an object, then there must exist an object type o^t and a model type MT_j that are part of an $\mu_{\mathbf{O}}$ mapping for y.

• If the value y of a statement is a data object then there must exist a datatype that is part of the range definition of the attribute in the meta model and there must be a mapping between the data type and the data object:

$$(x \ a \ y) \in \mathcal{T} \land y \in \mathbf{D} \Rightarrow$$

 $\exists d^t \in \mathbf{D}^T \ d^t \in \operatorname{range}(a) \land y \in \mu_{\mathbf{D}}(d^t)$ (24)

• If the value y of a statement is a model instance **mt**, then a model type **MT**_j must be part of the range definition and the y value must correspond to the mapping of that model type to the model instance:

$$(x \ a \ y) \in \mathcal{T} \land y \in \mathbf{mt} \Rightarrow$$

 $\exists \mathbf{MT}_i \in \operatorname{range}(a), y \in \mu_{\mathbf{mt}}(\mathbf{MT}_i)$ (25)

• For each statement the attribute *a* of that statement must be part of the same model type from which the object *x* has been mapped:

$$(x \ a \ y) \in \mathcal{T} \Rightarrow$$

 $\exists j \ a \in \mathbf{A}_j \land \exists o^t \in \operatorname{domain}(a), x \in \mu_{\mathbf{O}}(o^t, \mathbf{MT}_j)$
(26)

 If the value y of a statement is a data object then the data type must be part of the same model type as the attribute:

$$(x \ a \ y) \in \mathcal{T}, a \in \mathbf{A}_i, y \in \mathbf{D} \Rightarrow$$

$$\exists d^t \in \mathbf{D}_i^T, y \in \mu_{\mathbf{D}}(d^t)$$
 (27)

• And for the cardinality constraints: if $x \in \mu_{\mathbf{O}}(o^t, MT_j)$, $a \in \mathbf{A}_i$ where $\langle m, n \rangle = card(o^t, a)$ then $m \leq |\{y : (x \ a \ y) \in \mathcal{T} \land y \in (\mathbf{O} \cup \mathbf{D} \cup \mathbf{mt})\}| \leq n$.

4 APPLICATION OF FDMM TO THE 4R MODELING LANGUAGE

To illustrate the usage of the FDMM formalism we will show in the following how the modeling language from the running example in section 2.3 and instances of this modeling language can be formally described. We start by defining the model types that will represent the 4R portfolio models and 4R business process models by \mathbf{MT}_{PO} and \mathbf{MT}_{BP} :

$$\mathbf{MT}_{PO} = \left\langle \mathbf{O}_{PO}^{T}, \mathbf{D}_{PO}^{T}, \mathbf{A}_{PO} \right\rangle \tag{28}$$

$$\mathbf{MT}_{\mathrm{BP}} = \langle \mathbf{O}_{\mathrm{BP}}^{T}, \mathbf{D}_{\mathrm{BP}}^{T}, \mathbf{A}_{\mathrm{BP}} \rangle \tag{29}$$

Next, we detail the sets of object types $\mathbf{O}_{\text{SUP}}^T$, \mathbf{O}_{PO}^T and \mathbf{O}_{BP}^T for expressing what corresponds to the classes and relationclasses in ADOxx by:

$$\mathbf{O}_{PO}^{T} = \{Business-transaction, \\ relates-business-transaction\}$$

$$\mathbf{O}_{BP}^{T} = \{FlowObject, Start, Decision, Activity, \\ Parallelity, Join, End, 4R-event, \\ 4R-risk-aggregation, subsequent, aggregation,$$

Thereby, the object type FlowObject is defined as an abstract type that has to be instantiated through one of its sub types. In addition the following subtype relationships hold between the following object types:

in f luences}

$$Start \leq FlowObject$$
 $Decision \leq FlowObject$
 $Activity \leq FlowObject$
 $Parallelity \leq FlowObject$
 $Join \leq FlowObject$
 $End \leq FlowObject$ (31)

(30)

The same is applied for detailing the sets of data types \mathbf{D}_{PO}^{T} and \mathbf{D}_{BP}^{T} . Thereby, the **Enum**_{view} and **Enum**_{influence} types are used to represent the ADOxx enumeration attribute types with pre-defined values:

$$\mathbf{D}_{PO}^{T} = \{String, Float, \mathbf{Enum}_{view}\}$$

$$\mathbf{Enum}_{view} = \{Aggregated, Single\}$$

$$\mathbf{D}_{BP}^{T} = \{String, Float, \mathbf{Enum}_{influence}\}$$

$$\mathbf{Enum}_{influence} = \{Time\text{-}influence, Cost\text{-}influence,$$

$$Return\text{-}influence,$$

$$Quality\text{-}influence\}$$
(32)

We continue by detailing the sets of attributes A_{PO}

and \mathbf{A}_{BP} .:

$$\mathbf{A}_{PO} = \{ID, W, RE, RI, WE, \rho, relates-from, \\ relates-to, Process, View\}$$

$$\mathbf{A}_{BP} = \{Name, \varepsilon, I, Time, Cost, Return, Quality, \\ Influence-type, subsequent-from, \\ subsequent-to, aggregation-from, \\ aggregation-to, influences-from, \\ influences-to\}$$
(33)

For attaching the attributes to the object types and defining their value range, we add according domain and range definitions. This can be done for example by attaching the *Name* attribute to the required object type and then defining its range to be of the data type *String*. By using the *FlowObject* abstract type we can do this for all object types that are defined as its subtypes:

$$domain(Name) = \{FlowObject, 4R-risk-aggregation, \\ 4R-event\}$$

$$range(Name) = \{String\}$$
 (34)

We then add the cardinality definitions for each of the object types and their attributes as shown here exemplarily for the name attribute:

$$card(FlowObject,Name) = \langle 1,1 \rangle,$$

$$card(4R-risk-aggregation,Name) = \langle 1,1 \rangle,$$

$$card(4R-event,Name) = \langle 1,1 \rangle$$
 (35)

As it has been done for the attributes of the data type *String* we can similarly define the domain, range, and cardinality functions for an attribute of the type *Float*. As already mentioned above, the FDMM formalism does not further specify the data types so that we would have for example:

$$domain(W) = \{Business-transaction\}$$

$$range(W) = \{Float\}$$

$$card(Business-transaction, W) = \langle 0, 1 \rangle$$
 (36)

In the same way, ADOxx attributes with pre-defined values can be represented in FDMM as shown in the following by inserting the data type set **Enum**_{view} in the range definition to specify the type of view that is used for a business transaction:

domain(
$$View$$
) = { $Business-transaction$ }
range($View$) = { $Enum_{view}$ }
card($Business-transaction, View$) = $\langle 1, 1 \rangle$ (37)

To permit references from one object to another model instance, e.g. to reference business transactions

to corresponding 4R business process models, the following domain and range definitions are needed:

$$domain(Process) = \{Business-transaction\}$$
$$range(Process) = \{MT_{BP}\}$$

 $card(Business-transaction, Process) = \langle 0, 1 \rangle$ (38) Finally, we also give an example for defining the

Finally, we also give an example for defining the equivalent of a relationclass based on an object type that connects to two other object types via "to" and "from" attributes:

$$\begin{aligned} \operatorname{domain}(influences\text{-}from) &= \{influences\} \\ \operatorname{range}(influences\text{-}from) &= \{4R\text{-}risk\text{-}aggregation\} \\ \operatorname{card}(influences,influences\text{-}from) &= \langle 1,1 \rangle \\ \operatorname{domain}(influences\text{-}to) &= \{influences\} \\ \operatorname{range}(influences\text{-}to) &= \{Activity\} \\ \operatorname{card}(influences,influences\text{-}to) &= \langle 1,1 \rangle \\ \end{aligned}$$

Also for such an object type, that corresponds to a relation class, attributes can be added in the same way as shown above:

$$domain(Influence-type) = \{influences\}$$

$$range(Influence-type) = \{\mathbf{Enum}_{influence}\}$$

$$card(influences,Influence-type) = \langle 1,1 \rangle \tag{40}$$

When defining relation classes that can be used to connect multiple classes, the definition can be simplified by reverting to a supertype class as for example the *FlowObject* class and the *subsequent* relation class:

$$domain(subsequent-from) = \{subsequent\}$$

$$range(subsequent-from) = \{FlowObject\}$$

$$card(subsequent, subsequent-from) = \langle 1, 1 \rangle$$

$$domain(subsequent-to) = \{subsequent\}$$

$$range(subsequent-to) = \{FlowObject\}$$

$$card(subsequent, subsequent-to) = \langle 1, 1 \rangle$$

$$(41)$$

Based on these definitions for the model type we can describe the instantiation of a concrete model. As an example we use two models that have been described in (Fill et al., 2007) - see figures 3 and 4. They represent sample instances of a 4R portfolio model type and a 4R business process model type that shows how 4R events and 4R risk aggregations are used to represent the influence of risks on the accomplishment of activities. We will use these models to describe some of its contents by using the FDMM formalism.

First we instantiate concrete models for the model types \mathbf{MT}_{PO} and \mathbf{MT}_{BP} based on a mapping from the meta model definition:

$$\mu_{\mathbf{MT}}(\mathbf{MT}_{PO}) = \{\mathbf{mt}_{po1}\}$$

$$\mu_{\mathbf{MT}}(\mathbf{MT}_{BP}) = \{\mathbf{mt}_{bp1}\}$$
(42)

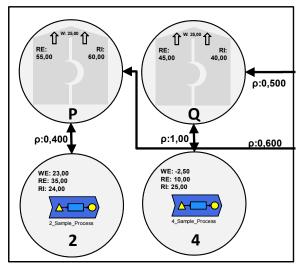


Figure 3: Excerpt of a 4R Portfolio Model (Fill et al., 2007)

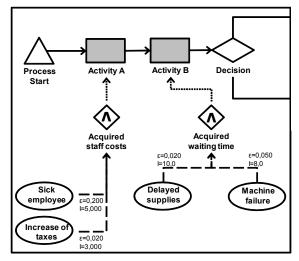


Figure 4: Excerpt of a 4R Business Process Model - translated from (Fill et al., 2007)

Next, we instantiate objects based on mappings from the object types. We show this exemplarily for some instances of the business transaction, activity, 4R event, and 4R aggregation object types:

$$\begin{split} \mu_{\mathbf{O}}(Business\text{-}transaction, \mathbf{MT}_{PO}) = & \{BT_{P}, BT_{Q}\} \\ \mu_{\mathbf{O}}(Activity, \mathbf{MT}_{BP}) = & \{Activity_{A}, \\ & Activity_{B}\} \end{split}$$

$$\mu_{\mathbf{O}}(4R\text{-}event, \mathbf{MT}_{BP}) = \{Machine\text{-}failure, \\ Delayed\text{-}supplies\} \}$$

$$\mu_{\mathbf{O}}(4R\text{-}aggregation, \mathbf{MT}_{BP}) = \{Acquired \\ -waiting\text{-}time\} \quad (43)$$

Similarly we can instantiate object types that can

later act as relations such as the influences type:

$$\mu_{\mathbf{O}}(influences, \mathbf{MT}_{BP}) = \{influences_1, influences_2\}$$
(44)

Subsequently, we also show the mappings of some data types to data objects in order to later assign them as values for attributes:

$$\mu_{\mathbf{D}}(String) = \{'ActivityA', 'ActivityB', \\ 'DelayedSupplies', \\ 'Machine failure', \\ Acquired-waiting-time \} \\ \mu_{\mathbf{D}}(Float) = \{25.00, 55.00, 60.00\} \\ \mu_{\mathbf{D}}(Time-influence) = \{'time-influence'\}$$
 (45)

And finally we can define the relationships between the objects and the data object by using the attributes in the form of triple statements, e.g. to express the names of concrete objects and the values of attributes and defining relations:

$$(Activity_A \ Name \ 'ActivityA') \in \beta(\mathbf{mt}_{bp1}),$$

$$(BT_P \ W \ 25.00) \in \beta(\mathbf{mt}_{po1}),$$

$$(influences_1 \ influences-from \ Acquired-waiting-time) \in \beta(\mathbf{mt}_{bp1}),$$

$$(influences_1 \ influences-to \ Activity_B) \in \beta(\mathbf{mt}_{bp1})$$

$$(46)$$

And for detailing the type of influence by specifying the attribute value that is available based on a predefined data type:

(influences₁ Influence-type 'time-influence')
$$\in \beta(\mathbf{mt}_{bp1})$$
(47)

5 DISCUSSION

With the description of the FDMM formalism it became possible for the first time to formally describe the core constituents of ADOxx based modeling languages. Thereby, the particular ways for defining meta models in ADOxx can now be analyzed and made available for comparisons with other meta modeling approaches. This concerns in particular the way how model types and relations between different model and class instances are represented. As a result, also mappings and transformations to other meta modeling approaches can now be facilitated using FDMM. In addition, FDMM can be of benefit especially for the further development of the Open Models Initiative and the numerous ADOxx modeling languages that are being developed by its projects.

As FDMM is able to formally describe the core ADOxx constituents but does not formalize the ADOxx approach as such, it has to be distinguished between the concepts as they are used within the ADOxx platform and the concepts as they are specified in the FDMM formalism. Due to the limitation of space we will here only discuss the main distinguishing features based on the set of eight categories of meta modeling concepts by (Kern et al., 2011). These categories are: characteristics of *first class concepts*, *relationships*, *attributes*, *inheritance*, *links to models*, *groupings*, and the type of *constraint language* used. In table 1 the values for the characteristics are shown.

It thus becomes obvious that concerning the first class concepts and the use of inheritance, FDMM is more generic than ADOxx. As the relationships are not described by first class objects in FDMM but by combinations of object types and attributes together will cardinalities – as shown e.g. in equation 39 – their arity is also set to n-ary. In ADOxx this is realized using interref attributes to connect to multiple objects. ADOxx further provides the constraint language ADOscript for checking and analyzing complex semantic constraints in models, which is currently not available in FDMM. Based on these characteristics ADOxx and FDMM can now also be compared to other meta modeling approaches. This will be discussed in section 6.

The application of FDMM to the 4R modeling language showed how the formalism can be used for a concrete example. Due to small number of constructs that are required for describing meta models and models in FDMM this could be easily accomplished. At the same time all parts of the modeling language could be successfully represented. Furthermore, in the context of the 4R modeling language the availability of a formal description is particularly beneficial for the definition of algorithms. It can now be easily determined which data types and structures are required for designing algorithms that perform calculations on the risk and return figures laid down in the 4R modeling language, and how they relate to the elements in the models. Based on the FDMM formalism such algorithms can now also be described independently of a concrete implementation.

6 RELATED WORK

When comparing FDMM and ADOxx to similar approaches in the literature, two directions can be taken. The first is the comparison to other meta modeling approaches and the second is the comparison to other kinds of formalizations for meta modeling ap-

proaches.

Based on the classification proposed by (Sprinkle et al., 2010), the FDMM and the ADOxx meta modeling approach directly compare to domain-specific modeling approaches that view meta models as language specifications. This is in contrast to approaches that treat meta models as software structure specifications, which is the typical use case for approaches such as EMOF (Object Management Group, 2011), EMF (McNeill, 2008) or KM3 (Jouault and Bezivin, 2006). A common aspect of domain-specific modeling approaches is the creation of visual model editors from meta models that are based on one predefined meta meta model and that use a graphical representation for the concrete syntax of the defined language. (Kern et al., 2011) also denote this direction as heavyweight approaches of language definition and distinguish it from lightweight approaches that adapt a generic meta model with domain-specific concepts. An example for the latter direction would be the use of the profile package in UML, e.g. to extend existing meta classes with the stereotyping mechanism (OMG, 2004).

In regard to the meta modeling concepts as shown in table 1, FDMM and ADOxx can be directly compared to the approaches analyzed in (Kern et al., 2011): thereby a core feature of ADOxx and FDMM that is shared with the GME and ARIS meta modeling approaches is the use of model types for defining the grouping of object types and their instances. In contrast to all approaches compared by Kern et al. and ADOxx, FDMM does not use any relation concept as a first class concept. Neither ADOxx nor FDMM use explicit *role type* concepts that provide further mechanisms for specifying relationships such as semantic dependencies between object types. However, in ADOxx such concepts can be expressed using the ADOscript language and enforced during modeling.

For the meta modeling approaches mentioned above, formalizations have been discussed for EMOF e.g. (Poernomo, 2006; Favre, 2010) and KM3 (Jouault and Bezivin, 2006). However, they differ from ADOxx in regard to their focus on the specification of software structures. Another approach that shows some similarities to the way the FDMM formalism has been conceived can also be found in the specification of the Object Constraint Language (OCL) (OMG, 2010)[Annex A]. However, the main difference is that FDMM is directed towards supporting the representation of meta models and models. The OCL specification does not describe a meta modeling approach but rather an approach to formalize one particular modeling language, i.e. UML together with constraints.

	ADOxx	FDMM
First Class Concepts	Model Type, Class, Relationclass	Model Type, Object Type, Data Type, Attribute
Arity of Relationships	n-ary (using interref)	n-ary
Attributes	single-value/multi-value	single-value/multi-value
Inheritance	single (Class only)	single (Object Types only)
Links to Models	yes	yes
Grouping	Model Types	Model Types
Constraint Language	ADOscript	none

Table 1: Comparison of Meta Modeling Concepts of ADOxx and FDMM

Furthermore, the domain, range, and card functions and the associated constraints described for them have a similarity with the notions of domain, range and cardinality restrictions used in in description logics (Baader, 2003). In contrast to the description logic case, our work is not intended to give a semantics for some formal language. Instead it is intended to provide a formal description of an existing system that has been effectively used in several application domains.

7 CONCLUSION AND OUTLOOK

In this paper we presented a formalism to describe the core constituents of the ADOxx meta modeling approach and showed its application to a concrete modeling language. It is the first formal definition for ADOxx meta modeling concepts and is therefore expected to be of benefit also for other projects using the ADOxx approach. Future work will therefore include the application to further modeling languages and the evaluation of the usability of the formalism. This concerns in particular the definition of algorithms, e.g. for describing analyses and simulations of models. Finally, it will also be investigated how the formalism can be represented visually to enhance the interaction with it and enable the easy re-use of formal meta model and model statements.

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